

Total No. of Printed Pages 8

4 SEM TDC ECO M 1

2014

(May)

ECONOMICS

(Major)

Course : 401

(Mathematics for Economics)

Full Marks : 80

Pass Marks : 32

Time : 3 hours

The figures in the margin indicate full marks
for the questions

1. Choose the correct answer : $1 \times 8 = 8$
- (a) $A \cup A'$ is (i) A (ii) A' (iii) Ω (iv) \emptyset

(3)

(b) Given $y = \log_{10} x$, $\frac{dy}{dx}$ is

- (i) $\log_{10} x$
- (ii) $\log_{10} e \times \frac{1}{x}$
- (iii) $\frac{1}{x^2}$
- (iv) $\frac{1}{x}$

(c) $\int_a^b f(x) dx = ?$

- (i) $-\int_b^a f(x) dx$
- (ii) $\int_b^a f(x) dx$
- (iii) $\int_0^b f(x) dx$
- (iv) $\int_a^0 f(x) dx$

(d) In the determinant $\begin{vmatrix} 9 & 8 & 7 \\ 6 & 5 & 4 \\ 3 & 2 & 1 \end{vmatrix}$, the minor

of the element 8 is

- (i) 0
- (ii) 8
- (iii) -3
- (iv) -6

14P—3600/899

(Continue)

(e) Given the AR function $AR = 10 - 0.5q$,
the MR function is

- (i) $MR = -0.5q^2$
- (ii) $MR = 10 - 0.5q^2$
- (iii) $MR = 10 - q$
- (iv) $MR = 10q - q$

(f) Rank of the matrix $\begin{bmatrix} 3 & 0 & 2 \\ -1 & 1 & 0 \\ 5 & 2 & 3 \end{bmatrix}$ is

- (i) 1
- (ii) 2
- (iii) 3
- (iv) 4

(g) The function $f(x) = \frac{x^2 + 3x - 4}{x - 1}$ is not continuous at

- (i) 1
- (ii) 2
- (iii) 3
- (iv) None of the above

(h) $\int a^x dx = ?$

- (i) $a^x + c$
- (ii) $\log a^x + c$
- (iii) $ax + c$
- (iv) $\frac{a^x}{\log_e a} + c$

14P—3600/899

(Turn Over)

2. Answer any four of the following :

(a) Find the numbers a and b that make $A^{4 \times 3}$ the inverse of B , when A

$$A = \begin{bmatrix} 2 & -1 & -1 \\ a & \frac{1}{4} & b \\ \frac{1}{8} & \frac{1}{8} & -\frac{1}{8} \end{bmatrix} \quad B = \begin{bmatrix} 1 & 2 & 4 \\ 0 & 1 & 6 \\ 1 & 3 & 2 \end{bmatrix}$$

(b) Illustrate Hawkins-Simon conditions

(c) Draw the graph of $xy = 1$

(d) Derive the elasticity of substitution for Cobb-Douglas production function.

(e) Evaluate :

$$\lim_{x \rightarrow 1} \frac{x^3 - 3x^2 + 2}{x^2 + 5x - 6}$$

(f) Given the input coefficient matrix

$$A = \begin{bmatrix} 0.05 & 0.25 & 0.34 \\ 0.33 & 0.10 & 0.12 \\ 0.19 & 0.38 & 0 \end{bmatrix}$$

Explain the economic meaning of the third column sum and the third row sum.

3. (a) (i) Define the following with examples : 1x4

Null set ; Disjoint set ; Convex set ; Union of sets

(ii) Define limit of a function.

14P—3600/899

(Continue)

14P—3600/899

(Turn Over)

(5)

(iii) A function is given by

$$y = \frac{x^2 - 4x + 3}{x^2 + 2x - 3}$$

find whether the function is continuous at $x = 1$ or not.

Or

(b) (i) If $A = \{2, 3, 4\}$, $B = \{2, 5, 6\}$; find $(A \cup B) \setminus (A \cap B)$

(ii) Solve the following pair of equations graphically :

$$x + 4y = 2$$

$$6x + 8y = 24$$

(iii) Define continuity of a function.

4. (a) (i) Consider the following macroeconomic model of two countries, $i = 1, 2$, that trade with each other :

$$Y_1 = C_1 + A_1 + X_1 - M_1, \quad C_1 = c_1 Y_1, \quad M_1 = m_1 Y_1$$

$$Y_2 = C_2 + A_2 + X_2 - M_2, \quad C_2 = c_2 Y_2, \quad M_2 = m_2 Y_2$$

Here $\forall i = 1, 2$; Y_i is income, C_i is consumption, A_i is (exogenous) autonomous expenditure, X_i denotes exports and M_i denotes imports of country i . Find the equilibrium values of Y_1 and Y_2 by matrix algebra.

(7)

Or

- (b) (i) A consumer has a utility function $u = u(x) = \alpha x^\beta$, $\alpha > 0$; $0 < \beta < 1$. Does the utility function display diminishing marginal utility? 5

- (ii) Find out $\frac{dy}{dx}$, when

$$y = \sqrt{\frac{1-x}{1+x}}$$

3

- (iii) The AR function is given by $AR = 100 - 3q$. Find the elasticity of demand at $q = 5$. 4

6. (a) (i) Find $\int x \ln x dx$.

- (ii) Given the MC function

$$MC = Q^2 - 4Q + 3$$

find the level of output (Q) at which the AVC will be minimum.

6

Or

- (b) (i) Given the marginal propensity to import $M'(Y) = 0.1$ and the information that $M = 20$ when $Y = 0$, find the import function $M(Y)$. 4

5. (a) Distinguish between Cobb-Douglas production function and CES production function. State and prove the properties of CES production function. 2+10=12

14P—3600/899

(Continued)

14P—3600/899

(Turn Over)

(ii) Define consumer's surplus. Give the demand function $p = 36 - q$ and the supply function $p = 6 + \frac{q^2}{4}$ find the consumer's surplus equilibrium.

7. (a) (i) Let the demand and supply functions be

$$Q_d = \alpha - \beta P + \sigma \frac{dP}{dt}, Q_s = -\gamma + \delta P$$

$$(\alpha, \beta, \gamma, \delta > 0)$$

Assuming that the rate of change of price over time is directly proportional to the excess demand, find the time path $P(t)$.

(ii) Briefly explain the use of differential equations in economics.

Or

(b) (i) In a market model

$$Q_{dt} = 12 - 2P_t$$

$$Q_{st} = -4 + 2P_{t-1}$$

$$\text{and } P_{t+1} - P_t = -0.25(Q_{st} - Q_{dt})$$

Find the time path P_t and test whether the time path is convergent.

(ii) Write a note on the cobweb model.

★ ★ ★